Internet Measurement and Data Analysis (7)

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2014-12-01

review of previous class

Class 6 Correlation (11/17)

- Online recommendation systems
- Distance
- Correlation coefficient
- exercise: correlation analysis

today's topics

Class 7 Multivariate analysis

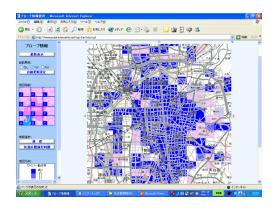
- Data sensing and GeoLocation
- Linear regression
- Principal Component Analysis
- exercise: linear regression
- assignment 2

data sensing

- data sensing: collecting data from remote site
- it becomes possible to access various sensor information over the Internet
 - weather information, power consumption, etc.

example: Internet vehicle experiment

- by WIDE Project in Nagoya in 2001
 - ▶ location, speed, and wiper usage data from 1,570 taxis
 - blue areas indicate high ratio of wiper usage, showing rainfall in detail



Japan Earthquake

- the system is now part of ITS
- usable roads info released 3 days after the quake
 - data provide by HONDA (TOYOTA, NISSAN)



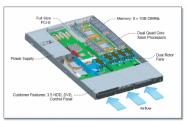
source: google crisis response

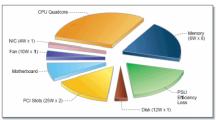
energy efficient technologies

- reduction in power consumption: issues in all technical fields
 - improving efficiency by intelligent control using sensor info
- from efficiency of individual equipment to efficiency of whole system
 - examples: PC servers and data centers

energy efficient PC servers

- intelligent control using sensor info within PC
 - temperature, voltage, power consumption, fan speed
- breakdown of PC server power consumption
 - ► CPU/memory: 50%
 - higher density, lower power, clock/voltage control
 - ▶ power supply: 20%
 - reduction in power loss (AC-DC, DC-DC)
 - ▶ IO: 20%
 - energy saving functions, energy efficient disks/SSD
 - cooling fans: 5%
 - better layout, air-flow design, optimized control





energy efficient data centers

- increasing power consumption by data centers with growing demands
 - contributed by cooling systems and power loss
- IT equipment: energy efficient equipment, use of servers with higher operating temperature
- cooling facility: spec reviews, air-flow/thermal-load design, energy efficient cooling equipment, free-air cooling
- power supply: loss reduction, high-voltage/DC power supply, energy efficient UPS, renewable energy
- total system design: adaptive control, human entry control, idle equipment shutdown



GeoLocation Services

- to provide different services according to the user location
- map, navigation, timetable for public transportation
- search for nearby restaurants or other shops (for advertisement)
- possibilities for other services

example: 駅.Locky (Eki.Locky)

- ▶ train timetable service by Kawaguchi Lab, Nagoya University
 - popular app from a WiFi GeoLocation research project
- App for iPhone/Android
- automatically select the nearest station and show timetable
 - geo-location by GPS/WiFi
 - also collect WiFi access point info seen by the device
- countdown for the next train
 - can show timetalbe as well
- crowdsourcing: timetable database contributed by users







GPS (Global Positioning System)

- about 30 satellites for GPS
- originally developed for US military use
 - for civilian use, the accuracy was intentionally degraded to about 100m
 - in 2000, the accuracy was improved to about 10m by removing intentional noise
- wide variety of civilian usage
 - car navigation, mobile phones, digital cameras
- location measurement: locate the position by distances from 3 GPS satellites
 - GPS signal includes satellite position and time information
 - distance is calculated by the difference in the time in the signal
 - needs 4 satellites to calibrate the time of the receiver
 - the accuracy improves as more satellites are used
- limitations
 - needs to see satellites
 - initialization time to obtain initial positioning
- improvements: combine with accelerometers, gyro sensors, wifi geo-location

geo-location using access points

- a communication device knows its associated access point
 - an access point also knows associated devices
 - a device can receive signals from non-associated access points
- there exit services to get location information from access points
- can be used indoors
 - other approaches: sonic signals, visible lights
- can be combined with GPS to improve accuracy

measurement metrics of the Internet

measurement metrics

- link capacity, throughput
- delay
- jitter
- packet loss rate

methodologies

- active measurement: injects measurement packets (e.g., ping)
- passive measurement: monitors network without interfering in traffic
 - monitor at 2 locations and compare
 - infer from observations (e.g., behavior of TCP)
 - collect measurements inside a transport mechanism

delay measurement

- delay components
 - delay = propagation delay + queueing delay + other overhead
 - ▶ if not congested, delay is close to propagation deley
- methods
 - round-trip delay
 - one-way delay requires clock synchronization
 - average delay
 - ightharpoonup max delay: e.g., voice communication requires <400ms
 - jitter: variations in delay

some delay numbers

- packet transmission time (so called wire-speed)
 - ▶ 1500 bytes at 10Mbps: 1.2msec
 - ▶ 1500 bytes at 100Mbps: 120usec
 - ▶ 1500 bytes at 1Gbps: 12usec
 - ▶ 1500 bytes at 10Gbps: 1.2usec
- speed of light in fiber: about 200,000 km/s
 - ▶ 100km round-trip: 1 msec
 - ▶ 20,000km round-trip: 200msec
- satellite round-trip delay
 - ▶ LEO (Low-Earth Orbit): 200 msec
 - ► GEO (Geostationary Orbit): 600msec

packet loss measurement

packet loss rate

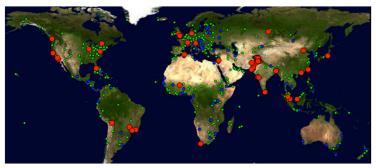
- loss rate is enough if packet loss is random...
- ▶ in reality,
 - bursty loss: e.g., buffer overflow
 - packet size dependency: e.g., bit error rate in wireless transmission

pingER project

- the Internet End-to-end Performance Measurement (IEPM) project by SLAC
- using ping to measure rtt and packet loss around the world
 - http://www-iepm.slac.stanford.edu/pinger/
 - ▶ started in 1995
 - over 600 sites in over 125 countries

pingER project monitoring sites

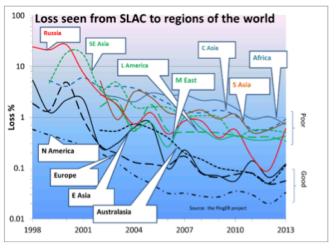
- monitoring (red), beacon (blue), remote (green) sites
 - beacon sites are monitored by all monitors



from pingER web site

pingER packet loss

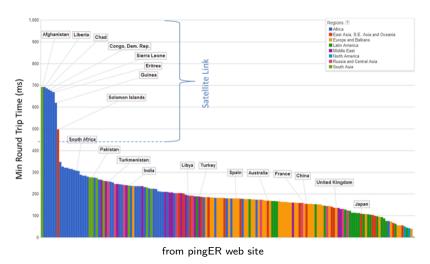
- packet loss observed from SLAC in the west coast
- exponential improvement in 15 years



from pingER web site

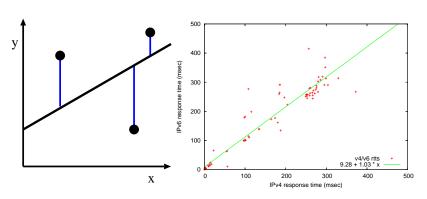
pinger minimum rtt

minimum rtts observed from SLAC in the west coast



linear regression

- fitting a straight line to data
 - ▶ least square method: minimize the sum of squared errors



least square method

a linear function minimizing squared errors

$$f(x) = b_0 + b_1 x$$

2 regression parameters can be computed by

$$b_1 = \frac{\sum xy - n\bar{x}\bar{y}}{\sum x^2 - n(\bar{x})^2}$$
$$b_0 = \bar{y} - b_1\bar{x}$$

where

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i \qquad \bar{y} = \frac{1}{n} \sum_{i=1}^{n} y_i$$
$$\sum xy = \sum_{i=1}^{n} x_i y_i \qquad \sum x^2 = \sum_{i=1}^{n} (x_i)^2$$

a derivation of the expressions for regression parameters

The error in the *i*th observation: $e_i = y_i - (b_0 + b_1 x_i)$ For a sample of n observations, the mean error is

$$\bar{e} = \frac{1}{n} \sum_{i} e_i = \frac{1}{n} \sum_{i} (y_i - (b_0 + b_1 x_i)) = \bar{y} - b_0 - b_1 \bar{x}$$

Setting the mean error to 0, we obtain: $b_0 = \bar{y} - b_1 \bar{x}$

Substituting b_0 in the error expression:

$$e_i = y_i - \bar{y} + b_1 \bar{x} - b_1 x_i = (y_i - \bar{y}) - b_1 (x_i - \bar{x})$$

The sum of squared errors, SSE, is

$$SSE = \sum_{i=1}^{n} e_i^2 = \sum_{i=1}^{n} [(y_i - \bar{y})^2 - 2b_1(y_i - \bar{y})(x_i - \bar{x}) + b_1^2(x_i - \bar{x})^2]$$

$$\frac{SSE}{n} = \frac{1}{n} \sum_{i=1}^{n} (y_i - \bar{y})^2 - 2b_1 \frac{1}{n} \sum_{i=1}^{n} (y_i - \bar{y})(x_i - \bar{x}) + b_1^2 \frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2$$
$$= \sigma_y^2 - 2b_1 \sigma_{xy}^2 + b_1^2 \sigma_x^2$$

The value of b_1 , which gives the minimum SSE, can be obtained by differentiating this equation with respect to b_1 and equating the result to 0:

$$\frac{1}{n}\frac{d(SSE)}{db_1} = -2\sigma_{xy}^2 + 2b_1\sigma_x^2 = 0$$

That is:
$$b_1 = \frac{\sigma_{xy}^2}{\sigma_z^2} = \frac{\sum xy - n\bar{x}\bar{y}}{\sum x^2 - n(\bar{x})^2}$$

principal component analysis; PCA

purpose of PCA

 convert a set of possibly correlated variables into a smaller set of uncorrelated variables

PCA can be solved by eigenvalue decomposition of a covariance matrix

applications of PCA

- demensionality reduction
 - sort principal components by contribution ratio, components with small contribution ratio can be ignored
- principal component labeling
 - find means of produced principal components

notes:

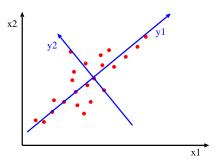
- PCA just extracts components with large variance
 - not simple if axes are not in the same unit
- a convenient method to automatically analyze complex relationship, but it does not explain the complex relationship

PCA: intuitive explanation

a view of cordinate transformation using a 2D graph

- draw the first axis (the 1st PCA axis) that goes through the centroid, along the direction of the maximal variability
- draw the 2nd axis that goes through the centroid, is orthogonal to the 1st axis, along the direction of the 2nd maximal variability
- draw the subsequent axes in the same manner

For example, "height" and "weight" can be mapped to "body size" and "slimness". we can add "sitting height" and "chest measurement" in a similar manner



PCA (appendix)

principal components can be found as the eigenvectors of a covariance matrix.

let X be a d-demensional random variable. we want to find a $d \times d$ orthogonal transformation matrix P that converts X to its principal components Y.

$$Y = P^{T}X$$

solve this equation, assuming cov(Y) being a diagonal matrix (components are independent), and P being an orthogonal matrix. $(P^{-1} = P^{\top})$ the covariance matrix of Y is

$$\begin{split} \mathit{cov}(Y) &=& \mathsf{E}[YY^\top] = \mathsf{E}[(P^\top X)(P^\top X)^\top] = \mathsf{E}[(P^\top X)(X^\top P)] \\ &=& \mathsf{P}^\top \mathsf{E}[XX^\top] \mathsf{P} = \mathsf{P}^\top \mathit{cov}(X) \mathsf{P} \end{split}$$

thus.

$$P\mathit{cov}(Y) = PP^{\top}\mathit{cov}(X)P = \mathit{cov}(X)P$$

rewrite P as a $d \times 1$ matrix:

$$P = [P_1, P_2, \dots, P_d]$$

also, cov(Y) is a diagonal matrix (components are independent)

$$cov(Y) = \begin{bmatrix} \lambda_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \lambda_d \end{bmatrix}$$

this can be rewritten as

$$[\lambda_1 P_1, \lambda_2 P_2, \dots, \lambda_d P_d] = [cov(X)P_1, cov(X)P_2, \dots, cov(X)P_d]$$

for $\lambda_i P_i = cov(X)P_i$, P_i is an eigenvector of the covariance matrix X thus, we can find a transformation matrix P by finding the eigenvectors.

previous exercise: computing correlation coefficient

- compute correlation coefficient using the sample data sets
 - correlation-data-1.txt, correlation-data-2.txt

correlation coefficient

$$\rho_{xy} = \frac{\sigma_{xy}^2}{\sigma_x \sigma_y} = \frac{\sum_{i=1}^n x_i y_i - \frac{(\sum_{i=1}^n x_i)(\sum_{i=1}^n y_i)}{n}}{\sqrt{(\sum_{i=1}^n x_i^2 - \frac{(\sum_{i=1}^n x_i)^2}{n})(\sum_{i=1}^n y_i^2 - \frac{(\sum_{i=1}^n y_i)^2}{n})}}$$

script to compute correlation coefficient

```
#!/usr/bin/env ruby
# regular expression for matching 2 floating numbers
re = /([-+]?\d+(?:\.\d+)?)\s+([-+]?\d+(?:\.\d+)?)/
sum x = 0.0 # sum of x
sum_v = 0.0 \# sum of v
sum xx = 0.0 # sum of x^2
sum_vy = 0.0 # sum of v^2
sum_xy = 0.0 \# sum of xy
n = 0 # the number of data
ARGF.each_line do |line|
   if re.match(line)
      x = $1.to f
     y = $2.to_f
     sum x += x
     sum v += v
     sum_xx += x**2
      sum_vy += v**2
      sum_xy += x * y
      n += 1
end
r = (sum_xy - sum_x * sum_y / n) /
 Math.sqrt((sum_xx - sum_x**2 / n) * (sum_yy - sum_y**2 / n))
printf "n:%d r:%.3f\n", n, r
```

previous exercise 2: similarity

- compute similarity in data
 - data from "Programming Collective Intelligence" Section 2
 - movie rating scores of 7 people: scores.txt

```
% cat scores.txt
# A dictionary of movie critics and their ratings of a small set of movies
'Lisa Rose': 'Lady in the Water': 2.5, 'Snakes on a Plane': 3.5, 'Just My Luck': 3.0, 'Superman Returns':
'Gene Seymour': 'Lady in the Water': 3.0, 'Snakes on a Plane': 3.5, 'Just My Luck': 1.5, 'Superman Return
'Michael Phillips': 'Lady in the Water': 2.5, 'Snakes on a Plane': 3.0, 'Superman Returns': 3.5, 'The Nig'
'Claudia Puig': 'Snakes on a Plane': 3.5, 'Just My Luck': 3.0, 'The Night Listener': 4.5, 'Superman Return
'Mick LaSalle': 'Lady in the Water': 3.0, 'Snakes on a Plane': 4.0, 'Just My Luck': 2.0, 'Superman Return
'Jack Matthews': 'Lady in the Water': 3.0, 'Snakes on a Plane': 4.0, 'The Night Listener': 3.0, 'Superman
'Toby': 'Snakes on a Plane': 4.5, 'You, Me and Dupree': 1.0, 'Superman Returns': 4.0
```

score data

- simplistic example: data is too small
- summarized in the following table

```
#name: 'Lady in the Water' 'Snakes on a Plane' 'Just My Luck' 'Superman Returns Lisa Rose:

2.5 3.5 3.0 3.5 3.0

Gene Seymour:
3.0 3.5 1.5 5.0 3.0

Michael Phillips:
2.5 3.0 - 3.5 4.0

Claudia Puig:
- 3.5 3.0 4.0 4.5

Mick LaSalle:
3.0 4.0 2.0 3.0 3.0

Jack Matthews:
3.0 4.0 - 5.0 3.0

Toby:
- 4.5 - 4.0 -
```

similarity computation

create a similarity matrix using cosine similarity

```
% ruby similarity.rb scores.txt
Lisa Rose: 1.000 0.959 0.890 0.921 0.982 0.895 0.708
Gene Seymour: 0.959 1.000 0.950 0.874 0.962 0.979 0.783
Michael Phillips: 0.890 0.950 1.000 0.850 0.929 0.967 0.693
Claudia Puig: 0.921 0.874 0.850 1.000 0.875 0.816 0.695
Mick LaSalle: 0.982 0.962 0.929 0.875 1.000 0.931 0.727
Jack Matthews: 0.895 0.979 0.967 0.816 0.931 1.000 0.822
Toby: 0.708 0.783 0.693 0.695 0.727 0.822 1.000
```

similarity computation script (1/2)

```
# regular expression to read data
# 'name': 'title0': score0, 'title1': score1, ...
re = /'(.+?)': \s+(\S.*)/
name2uid = Hash.new # keeps track of name to uid mapping
title2tid = Hash.new # keeps track of title to tid mapping
scores = Hash.new # scores[uid][tid]: score of title id by user id
# read data into scores[uid][tid]
ARGF.each line do |line|
  if re.match(line)
    name = $1
    ratings = $2.split(".")
    if name2uid.has_key?(name)
      uid = name2uid[name]
    else
      uid = name2uid.length
      name2uid[name] = uid
      scores[uid] = {} # create empty hash for title and score pairs
    end
    ratings.each do |rating|
      if rating.match(/'(.+?)':\s*(\d\.\d)/)
        title = $1
       score = $2.to f
        if title2tid.has kev?(title)
          tid = title2tid[title]
        else
          tid = title2tid.length
          title2tid[title] = tid
        end
        scores[uid][tid] = score
      end
    end
  end
and
```

similarity computation script (2/2)

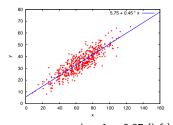
```
# compute cosine similarity between 2 users
def comp similarity(h1, h2)
 sum_xx = 0.0 # sum of x^2
 sum_vv = 0.0 # sum of v^2
 sum xv = 0.0 # sum of xv
 score = 0.0 # similarity score
 h1.each do |tid. score|
    sum xx += score**2
   if h2.has_key?(tid)
      sum_xy += score * h2[tid]
    end
  end
 h2.each_value do |score|
    sum vv += score**2
  end
 denom = Math.sqrt(sum_xx) * Math.sqrt(sum_yy)
  if denom != 0.0
   score = sum xv / denom
  end
 return score
end
# create n x n matrix of similarities between users
n = name2uid.length
similarities = Array.new(n) { Array.new(n) }
for i in 0 .. n - 1
 printf "%-18s", name2uid.kev(i) + ':'
 for i in 0 .. n - 1
    similarities[i][j] = comp_similarity(scores[i], scores[j])
   printf "%.3f ", similarities[i][j]
 end
 print "\n"
end
```

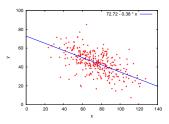
today's exercise: linear regression

- linear regression by the least square method
- use the data for the previous exercise
 - correlation-data-1.txt, correlation-data-2.txt

$$f(x) = b_0 + b_1 x$$

$$b_1 = \frac{\sum xy - n\bar{x}\bar{y}}{\sum x^2 - n(\bar{x})^2}$$
$$b_0 = \bar{y} - b_1\bar{x}$$





data-1:r=0.87 (left), data-2:r=-0.60 (right)

script for linear regression

```
#!/usr/bin/env rubv
# regular expression for matching 2 floating numbers
re = /([-+]?\d+(?:\.\d+)?)\s+([-+]?\d+(?:\.\d+)?)/
sum_x = sum_y = sum_xx = sum_xy = 0.0
n = 0
ARGF.each line do |line|
    if re.match(line)
      x = $1.to f
      y = $2.to_f
      sum_x += x
      sum_y += y
      sum_xx += x**2
      sum_xy += x * y
      n += 1
    end
end
mean x = Float(sum x) / n
mean_v = Float(sum_v) / n
b1 = (sum_xy - n * mean_x * mean_y) / (sum_xx - n * mean_x**2)
b0 = mean v - b1 * mean x
printf "b0:%.3f b1:%.3f\n", b0, b1
```

adding the least squares line to scatter plot

```
set xrange [0:160]
set yrange [0:80]

set xlabel "x"
set ylabel "y"

plot "correlation-data-1.txt" notitle with points, \
5.75 + 0.45 * x lt 3
```

assignment 1: the finish time distribution of a marathon

- purpose: investigate the distribution of a real-world data set
- data: the finish time records from honolulu marathon 2013
 - http://www.pseresults.com/events/568/results
 - ▶ the number of finishers: 22,089
- items to submit
 - mean, standard deviation and median of the total finishers, male finishers, and female finishers
 - 2. the distributions of finish time for each group (total, men, and women)
 - plot 3 histograms for 3 groups
 - use 10 minutes for the bin size
 - use the same scale for the axes to compare the 3 plots
 - 3. CDF plot of the finish time distributions of the 3 groups
 - plot 3 groups in a single graph
 - 4. discuss differences in finish time between male and female. what can you observe from the data?
 - 5. optional
 - other analysis of your choice (e.g., discussion on differences among age groups)
- submission format: a single PDF file including item 1-5
- submission method: upload the PDF file through SFC-SFS
- submission due: 2014-11-19 (extended)

honolulu marathon data set

data format

Pla	ace Num		Lname	Fname	Country	Division						21Km	30Km	40Km
		Time					Plc	o Tot	P1c	c Total	1			
1	6	2:18:47	Chepkwony	Gilbert	KEN	MElite	1	8	1	11789	0:34:24	1:11:42	1:40:41	2:12:14
2	2	2:19:22	Chelimo	Nicholas	KEN	MElite	2	8	2	11789	0:34:25	1:11:43	1:40:41	2:12:40
3	7	2:19:38	Bushendich	Solomon	KEN	MElite	3	8	3	11789	0:34:25	1:11:43	1:40:41	2:12:51
4	4	2:20:09	Adihana	Gebretsadi	ik ETH	MElite	4	8	4	11789	0:34:24	1:11:42	1:40:41	2:13:16
5	8	2:20:25	Kimutai	Kiplimo	KEN	MElite	5	8	5	11789	0:34:25	1:11:42	1:40:41	2:13:21
6	1	2:21:16	Lel	Martin	KEN	MElite	6	8	6	11789	0:34:24	1:11:42	1:40:41	2:13:51
7	5	2:21:51	Tadesse	Abraham	ERI	MElite	7	8	7	11789	0:34:24	1:11:42	1:40:41	2:14:27
8	45	2:22:52	Jefferson	Fidele	USA	M35-39	1	1315	8	11789	0:34:24	1:11:43	1:40:49	2:15:29
9	25742	2:23:20	Tsukamoto	Shuji	JPN	M30-34	1	1279	9	11789	0:34:22	1:11:40	1:40:52	2:15:52
10	25767	2:31:13	Hino	Yuya	JPN	M20-24	1	702	10	11789	0:34:22	1:12:25	1:45:10	2:22:57

- Chip Time: finish time
- ► Category: MElite, WElite, M15-19, M20-24, ..., W15-29, W20-24, ...
 - note some runners have "No Age" for Category
- ► Country: 3-letter country code: e.g., JPN, USA
- check the number of the total finishers when you extract the finishers

item 1: computing mean, standard deviation and median

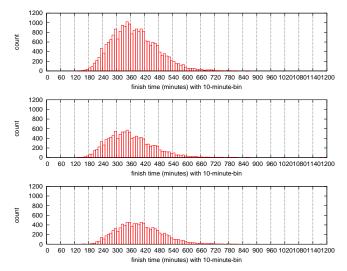
- round off to minute (slightly different from using seconds)
- classify "No Age" using "Sex Total"

	n	mean	stddev	median
all	22,089	376.8	98.2	367
men	11,789	359.3	96.8	348
women	10,300	397.0	95.8	389

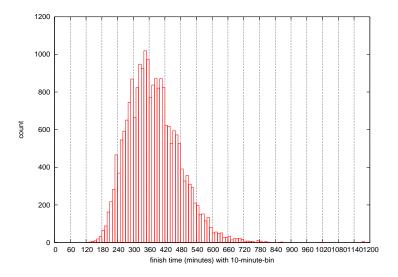
example script to extract data

item 2: histograms for 3 groups

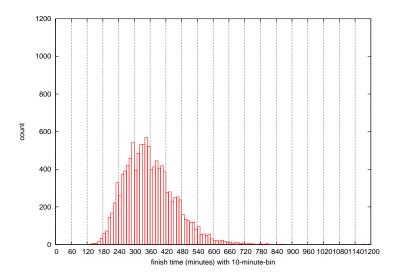
- plot 3 histograms for 3 groups
- use 10 minutes for the bin size
- use the same scale for the axes to compare the 3 plots



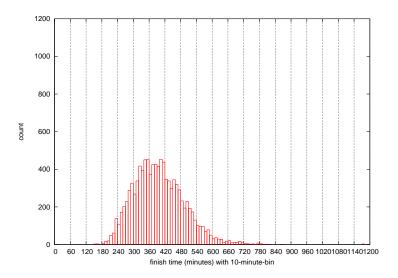
histograms for all



histograms for men

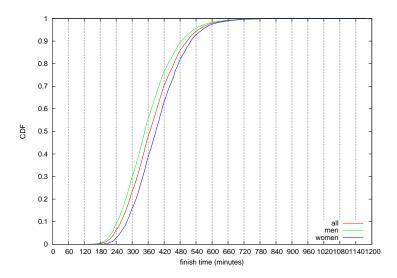


histograms for women



item 3: CDF of the finish time distributions of the 3 group

plot 3 groups in a single graph



assignment 2: twitter data analysis

- purpose: processing realworld big data
- data sets:
 - twitter data for about 40M users by Kwak et al. in July 2009
 - http://an.kaist.ac.kr/traces/WWW2010.html
 - twitter_degrees.zip (164MB, 550MB uncompressed)
 - user_id, followings, followers
 - numeric2screen.zip (365MB, 756MB uncompressed)
 - user_id, screen_name
- items to submit
 - CCDF plot of the distributions of twitter users' followings/followers
 - ▶ log-log plot, the number of followings/followers on X-axis
 - 2. list of the top 30 users by the number of followers
 - rank, user_id, screen_name, followings, followers
 - optional
 - other analysis of your choice
 - 4. discussion
 - describe what you observe from the data
- submission: upload your report in the PDF format via SFC-SFS
- submission due: 2014-12-17 (Wed)

twitter data sets

twitter_degrees.zip (164MB, 550MB uncompressed)

id followings followers

```
12
        586
                 1001061
13
        243
                 1031830
14
        106
                 8808
15
        275
                14342
16
        273
                 218
17
        192
                 6948
18
        87
                 6532
20
        912
                1213787
21
        495
                 9027
22
        272
                 3791
```

. . .

numeric2screen.zip (365MB, 756MB uncompressed)

id screenname

```
12 jack
```

20 ev

21 dom 22 rabble

. . .

¹³ biz

¹⁴ noah 15 crystal

¹⁰ CI y 5 C

¹⁶ jeremy

¹⁷ tonystubblebine

¹⁸ Adam

items to submit

CCDF plot

- ▶ log-log plot, the number of followings/followers on X-axis
- plot the 2 distributions in a single graph

list of the top 30 users by the number of followers

- rank, user_id, screen_name, followings, followers
- you need to sort and merge 2 files

#	rank	id	screenname	followings	followers
1 2		19058681 15846407	aplusk TheEllenShow	183 26	2997469 2679639
3		16409683	britneyspears	406238	2674874
4 5		428333	cnnbrk	18	2450749 1994926
6		19397785 783214	Oprah twitter	15 55	1959708

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sort command

sort command: sorts lines in a text file

```
$ sort [options] [FILE ...]
```

- options (relevant to the assignment)
 - -n : compare according to string numerical value
 - -r : reverse the result of comparisons
 - -k POS1[,POS2]: start a key at POS1, end it at POS 2 (origin 1)
 - ▶ -t SEP : use SEP instead of non-blank as the field-separator
 - -m : merge already sorted files
 - -T DIR : use DIR for temporary files

example: sort "file" using the 3rd field as numeric value in the reverse order , use "/usr/tmp" for temporary files

```
$ sort -nr -k3,3 -T/usr/tmp file
```

summary

Class 7 Multivariate analysis

- Data sensing and GeoLocation
- Linear regression
- Principal Component Analysis
- exercise: linear regression
- assignment 2

next class

Class 8 Time-series analysis (12/8)

- Internet and time
- Network Time Protocol
- ► Time series analysis
- exercise: time-series analysis